20MA210E					Numerical Methods					
Teaching Scheme					Examination Scheme					
L	Т	Р	С	Hrs. /Week	Theory			Practical		Total
					MS	ES	IA	LW	LE/Viva	Marks
3	0	0	3	3	25	50	25			100

### **COURSE OBJECTIVES**

- > To understand and acquaint the concept of various numerical methods.
- To develop numerical skills in solving problem of engineering interest.
- To lay foundation of computational techniques for post graduate/specialized studies and research.
- To make familiar the numerical solution techniques for linear/nonlinear ODEs/PDEs.

### UNIT 1 SOLUTION OF SIMULTANEOUS LINEAR EQUATIONS AND INTERPOLATION

10 Hrs.

Iterative methods: Gauss-Jacobi's method, Gauss-Seidel method, Numerical evaluation of largest as well as smallest (numerically) Eigen values and corresponding Eigen vectors.

Introduction to interpolation, Newton Gregory Forward Interpolation Formula, Newton Gregory Backward Interpolation Formula, Central difference interpolation formula, Lagrange's Interpolation Formula for unevenly spaced Formula, Error in interpolation, Newton's Divided Difference Formula, cubic spline interpolation.

### **UNIT 2 NUMERICAL DIFFERENTIATION AND INTEGRATION**

10 Hrs.

Introduction, Formulae for Derivatives, Newton-Cotes' Quadrature Formula, Trapezoidal rule, Simpson's rule, Weddle's rule, Romberg's method, error in integration, Double Integration with constant and variable limits, Gaussian integration.

## UNIT 3 NUMERICAL SOLUTION OF ORDINARY DIFFERENTIAL EQUATIONS AND TRANSCENDENTAL EQUATIONS

10 Hrs.

Runge-Kutta methods of various order, Modified Euler's method, Predictor corrector method: Adam's method, Milne's method, Solution of Boundary value problems using finite differences, Fixed Point Iteration Method, Newton's Method.

# **UNIT 4 NUMERICAL SOLUTION OF PARTIAL DIFFERENTIAL EQUATION**

10 Hrs.

Finite difference approximation of partial derivatives, Classification of 2nd order PDEs, different type of boundary conditions, solutions of Elliptic, parabolic and hyperbolic equations of one and two dimensions, Crank- Nicholson method, ADI method.

40 Hrs.

## **COURSE OUTCOMES**

On completion of the course, student will be able to

- CO1 Apply a suitable numerical technique to extract approximate solution to the problem whose solution cannot be obtained by routine methods.
- CO2 Analyze the accuracy of numerical methods by estimating error.
- CO3 Analyze / interpret the achieved numerical solution of problems by reproducing it in graphical or tabular form.
- CO4 Evaluate a polynomial on which operations like division, differentiation and integration can be done smoothly from the data generated by performing an experiment or by an empirical formula.
- CO5 Evaluate a sufficiently accurate solution of various physical models of science as well as engineering interest whose governing equations can be approximated by nonlinear ODEs or PDEs or system of ODEs or PDEs.
- CO6 Design / create an appropriate numerical algorithm for various problems of science and engineering.

## **TEXT/REFERENCE BOOKS**

- 1. B.S. Grewal, Numerical Methods in Engineering and Science with Programs in C & C++, Khanna Publishers, 2010.
- 2. S.S. Sastry, Introductory Methods for Numerical Analysis, 4<sup>th</sup> ed., Prentice Hall of India, 2009.
- 3. M.K. Jain, S.R.K. Iyengar, R.K. Jain, Numerical Methods for Scientific and Engineering Computation, New Age International, 2007.
- 4. C. F. Gerald and P. O. Wheatley, Applied Numerical analysis, 7<sup>th</sup> ed., Pearson education, 2003.
- 5. Erwin Kreyszig, Advanced Engineering Mathematics, 9<sup>th</sup> ed., Wiley publication, 2005
- 6. R.K. Jain & S.R.K. Iyengar, Advanced Engineering Mathematics, 3<sup>rd</sup> ed., Narosa, 2002.