| 20MSM509T       |   |   |   |             | Тороlоду           |    |    |           |         |       |
|-----------------|---|---|---|-------------|--------------------|----|----|-----------|---------|-------|
| Teaching Scheme |   |   |   |             | Examination Scheme |    |    |           |         |       |
| L               | т | Р | с | Hrs. / Week | Theory             |    |    | Practical |         | Total |
|                 |   |   |   |             | MS                 | ES | IA | LW        | LE/Viva | Marks |
| 3               | 1 | 0 | 4 | 4           | 25                 | 50 | 25 |           |         | 100   |

# **COURSE OBJECTIVES**

To be able to gain knowledge of topological spaces with different characteristics.

> To be able to work out the product of two spaces and the role of bounded sets in pure mathematics

- ➤ To be able to relate the compactness and different sets.
- > To study separable and regularity axioms and their significance.

# **UNIT 1 TOPOLOGICAL SPACES**

Pandit Deendayal Energy University

Topological Spaces, Bases, Subspace, Closed Sets, Open Sets, Interior, Closure, Limit point, Boundary of a set. T1, T2-spaces, Continuous functions, Pasting Lemma

#### **UNIT 2 PRODUCT SPACES AND BOUNDED SETS**

Product space, Projections, Weak topology, Product of T1, T2-spaces, Metric topology, Basicconcepts and sequences, Continuity and uniform continuity, Bounded subsets, Totally boundedsubsets.

### **UNIT 3 COMPACT SPACES**

Compact topological spaces, Finite Intersection Properties, Hausdorff and Compactness, Compact metric spaces, Heine-Borel Theorem.

#### UNIT 4 REGULAR, COUNTABLE AND SEPARABLE SPACES

Regular, Normal, Completely regular spaces, Compact Hausdorff spaces, Second Countablespace, separable space, second Countability and Separability in metric space.

# **COURSE OUTCOMES**

On completion of the course, student will be able to

- CO1 Identify variety of spaces in Topological aspect.
- CO2 Understand the concept of closed and opens sets in different contexts and continuous functions in topology. .
- CO3 Explain various metric topologies and demonstrate the uniform continuity.

CO4 – Analyze the compactness of a topological space and to justify whether the space is Hausdorff or not.

CO5 – Appraise the significance of Heine-Borel theorem and the connection with different topological spaces.

CO6 – Evaluate regularity, countability and separability of various spaces.

# **TEXT/REFERENCE BOOKS**

- 1. Simmons G F, Introduction to Topology and Modern Analysis, McGraw-Hill Co., Tokyo, 1963.
- 2. Munkres, J, Topology: A First Course, Prentice Hall of India Pvt. Ltd., New Delhi, 2000.
- 3. Kumaresan S., Topology of Metric Spaces, Narosa Publication, New Delhi, 2011.
- 4. Joshi K.D., Introduction to General Topology, New Age Publishers, New Delhi, 1983.

### 40 Hrs.

# 12 Hrs.

10 Hrs.

School of Technology

# 08 Hrs.

10 Hrs.

#### 40...